

# Value Driven Landmarks for Oversubscription Planning

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June 24, 2018

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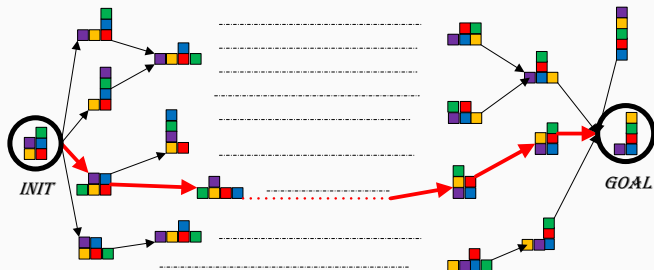
## Background

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## Classical Planning Problem

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### Objective

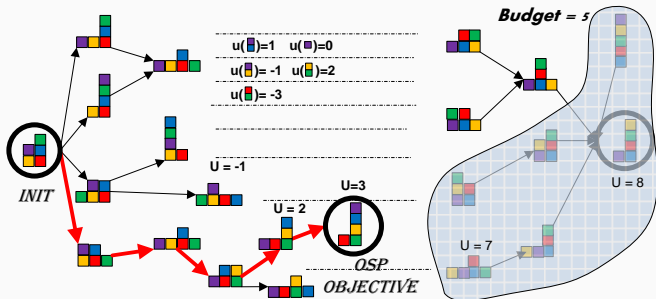
Find a sequence of actions from a given initial state to achieve a **goal state**

### Optimal Classical Planning

constrained to the **cheapest** cost sequence of actions which achieves the goal



## Oversubscription (OSP) Planning Problem



### Objective

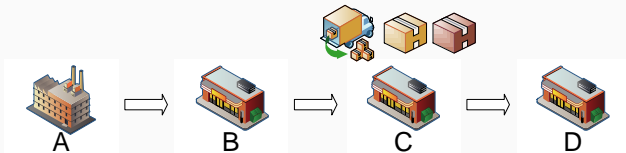
Find a sequence of actions from a given initial state to a **valuable state**, within a **limited budget** on action cost

### Optimal OSP

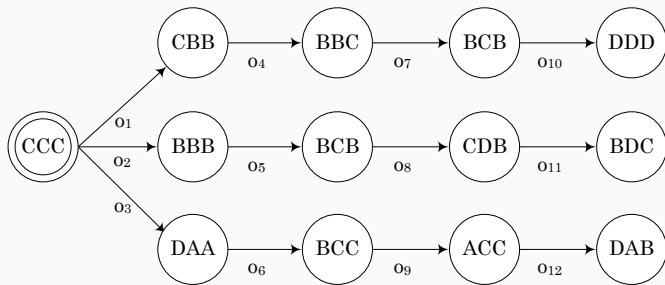
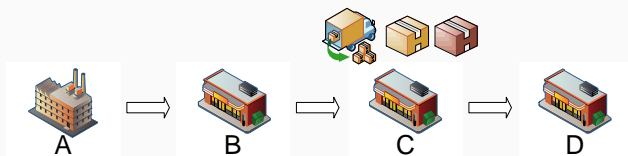
Constrained to finding a sequence of actions which achieves a state with **maximal utility**

## Logistics Task - Search Space Example

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## Logistics Task - Search Space Example



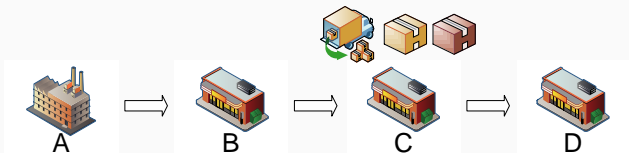
## Formalism

### Classical Planning

$$\Pi = \langle V, s_0, G; A, c \rangle$$

### Oversubscription Planning (OSP)

$$\Pi = \langle V, s_0, u; A, c, b \rangle$$



### State Variables

- $V = \{v_1, \dots, v_n\}$ .
- $S = \text{dom}(v_1) \times \dots \times \text{dom}(v_n)$ .

### Initial State

- $s_0 \in S$ .

### Actions

- $A = \{a_1, \dots, a_n\}$ .
- Each  $a \in A$  represented by a pair;
  - $\langle \text{pre}(a), \text{eff}(a), c \rangle$ .
- $\text{pre}(a), \text{eff}(a)$  are partial assignments to  $V$ .

## Formalism

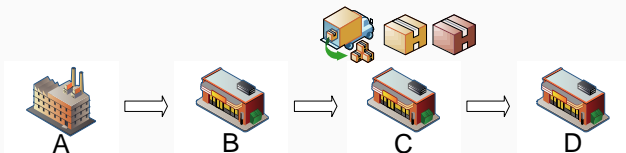
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### Classical Planning

$$\Pi = \langle \mathbf{V}, \mathbf{so}, G; \mathbf{A}, \mathbf{c} \rangle$$

### Oversubscription Planning (OSP)

$$\Pi = \langle \mathbf{V}, \mathbf{so}, u; \mathbf{A}, \mathbf{c}, b \rangle$$



### Initial State Representation

- $v_{truck1} = at(truck1, loc-A)$
- $v_{pkg1} = at(pkg1, loc-A)$
- $v_{pkg2} = at(pkg2, loc-A)$

### Action Representation

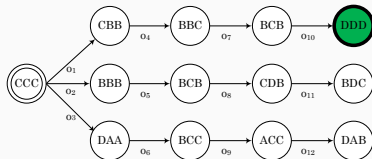
- $a = load-truck\ pkg1\ truck1\ loc-A$
- $pre(a) = \{at(pkg1, loc-A)\}$
- $eff(a) = \{in(pkg1, truck1)\}$
- $c(a) = 1$

## Hard Goals vs. Utility&Budget

### Classical Planning

$$\Pi = \langle V, s_0, \mathbf{G}; A, c \rangle$$

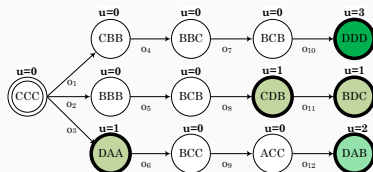
- $G$  is a partial assignment on state variables
- $G \subseteq V$ .



### Oversubscription Planning (OSP)

$$\Pi = \langle V, s_0, \mathbf{u}; A, c, \mathbf{b} \rangle$$

- $u$  is a **state utility** function  
 $u : S \rightarrow \mathbb{R}$ .
- $b \in \mathbb{R}^{0+}$  is an **cost budget** allowed for the task over **actions**.

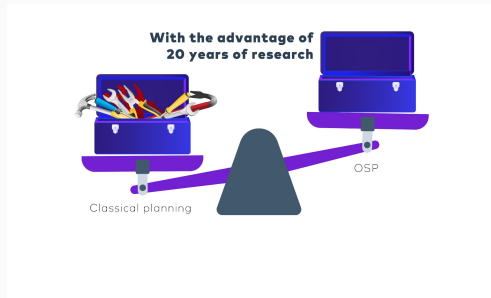


## Recent Advances in Heuristic Search OSP

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### Smith, 2004

- presented the OSP problem

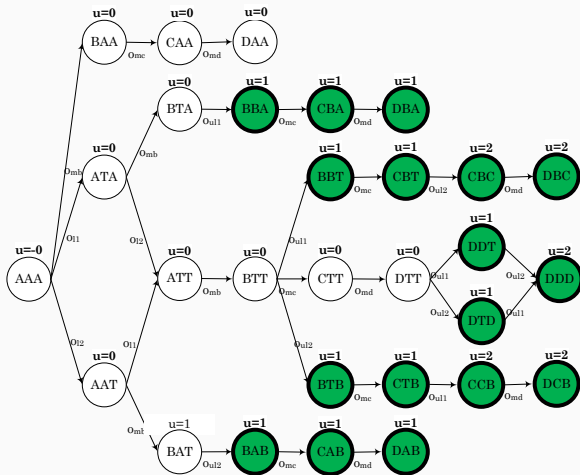


### Mirkis and Domshlak, 2014

- Logical landmarks for goal reachability ("Bring me Something")
- Budget Reduction

# "Bring me Something" Landmarks in OSP - Logistics Task

Budget = 4







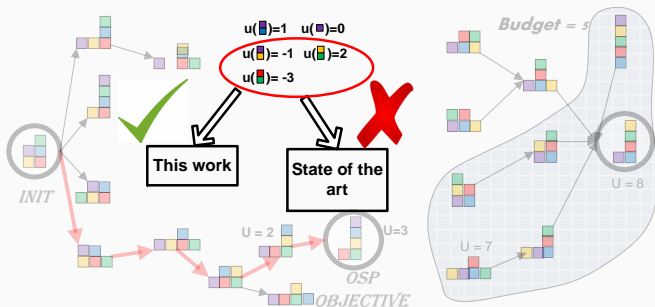




## The Gap in Heuristic OSP Search

### Limited Expressivity

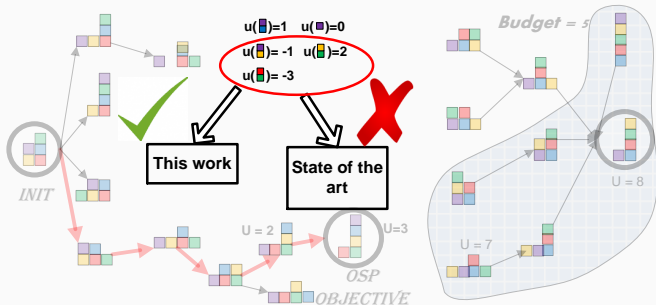
- 0-binary utility functions
- non-negative utility



## Bridge The Gap in Heuristic OSP Search

### Arbitrary Additive Utility Functions

- non 0-binary utility functions
- negative utility functions



## Motivation & Challenges

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## Why Negative Values Effects Need a Special Treatment?

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### Classical Planing & Non-Negative OSP

Strive to collect the goals (or valuable facts) which are a partial assignment to state variables



## Why Negative Values Effects Need a Special Treatment?

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### General OSP

Consider an entire state

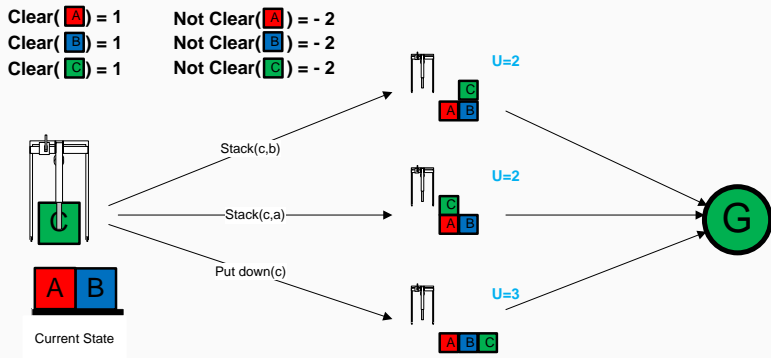
Avoiding collection of facts carrying negative values





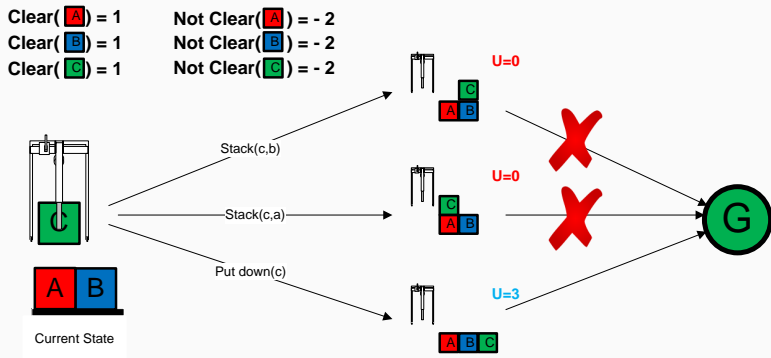
## In State Negative Interactions Between Facts

When the focus is on goal or valuable facts, we have 3 goal states



## In State Negative Interactions Between Facts

When considering a wider set of facts, we stay with one goal state



## Good is not Enough

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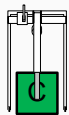
### Negative Interactions Between States

When the focus is just on target state, we have a goal

Clear(A) = 10

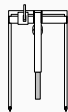
Clear(B) = 1

Clear(C) = 5



Current State

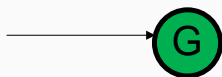
Stack(c,a)



U = 6



Current State



## In OSP we want Better

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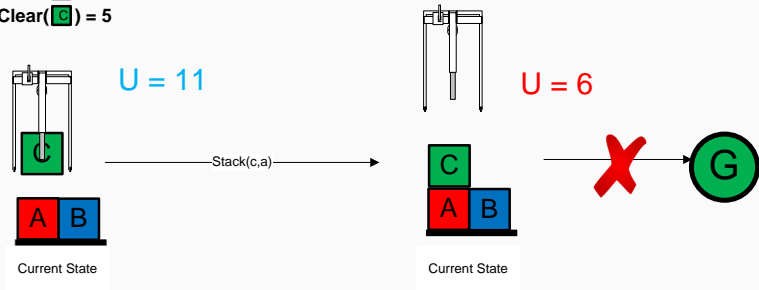
### Negative Interactions Between States

When we consider also action origin state, it seems to be less attractive

Clear(**A**) = 10

Clear(**B**) = 1

Clear(**C**) = 5



## Relative Evaluation of Achievements

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Focus on **improving** state-variables rather than on **collecting** valuable facts:

- **characterization** of the **process** of searching for an improvement  
we define the **utility of actions**
  - exploiting descriptiveness of actions
  - discover **properties** of optimal plans on the level of **actions** and **sequences of actions**
  - synergistic combination of these properties allows handling **arbitrary additive utility** functions over multi-valued variables
  - define an effective search space

## Relative Evaluation of Achievements

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Focus on **improving** state-variables rather than on **collecting** valuable facts:

- **characterization** of the **process** of searching for an improvement
- Relative evaluation of plans (eliminate dependence on initial state)
  - **dynamic reference** point for improvement
  - **optimal** and **satisficing** planning
- treat real-world **investment scenarios**
- domain and utility setting independent

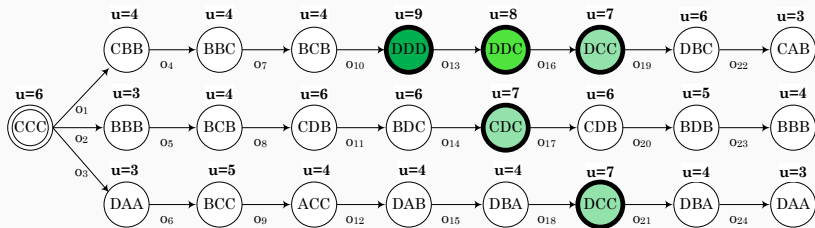
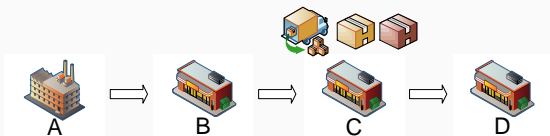
## Optimal Plan Properties

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## High Level Overview

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## Utility Function Definition for Actions

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### Definition

For an OSP action  $a$ , the **net utility** of  $a$  is

$$u_a^{net}(a) = \sum_{v \in \mathcal{V}(\text{eff}(a))} [u_v(\text{eff}(a)[v]) - u_v(\text{pre}(a)[v])]$$

## Utility Function Definition for Actions

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### Definition

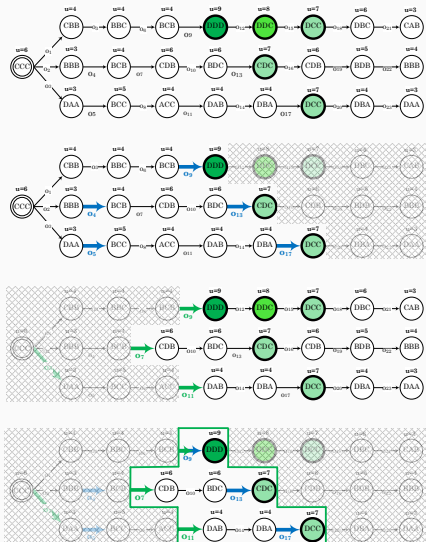
For an OSP action  $a$ , the **net utility** of  $a$  is

$$u_a^{net}(a) = \sum_{v \in \mathcal{V}(\text{eff}(a))} [u_v(\text{eff}(a)[v]) - u_v(\text{pre}(a)[v])]$$

### Captures State Dependencies

- Traces total benefit of an action with respect to its origin state
- In OSP, goal could be achieved just through an action with total positive net value

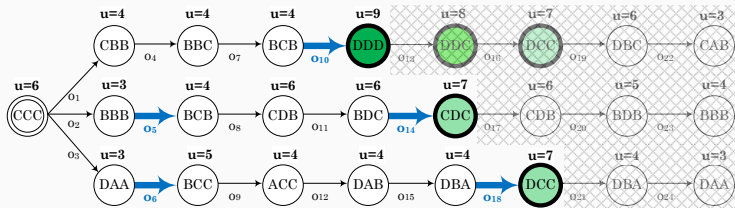
# High Level Overview - Improving Approach



## Net Positive Suffix Termination

For each plan  $\pi$ , there is plan  $\pi'$  that:

- ends with a net positive utility value action  $a_{last}$ ,
- is at most as costly as  $\pi$ , and
- is at least as valuable as  $\pi$



## Improving Approach

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### Dynamic Reference Point to Improve

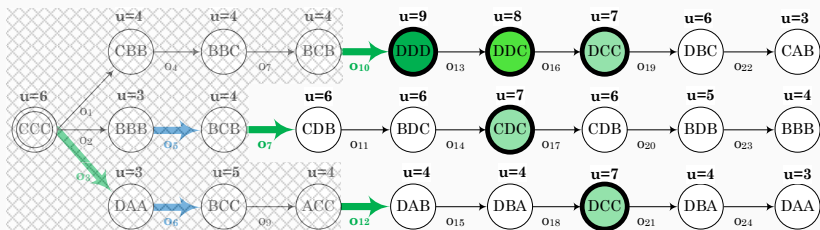
Given an OSP task  $\Pi = \langle V, s_0, u; A, c, b \rangle$  and a state  $s$ , let **improved**( $s$ ) be the set of all propositions  $\langle v/d \rangle \in \mathcal{D}$  such that  $u_v(d) > u_v(s[v])$ .

### Gross Positive Actions

Given an OSP task  $\Pi = \langle V, s_0, u; A, c, b \rangle$  and a state  $s$ , the **gross positive actions** relative to  $s$   $A_{gPos}(s) \subseteq A$  of  $\Pi$  are  $A_{gPos}(s) = \{a \in A, \text{eff}(a) \cap \text{improved}(s) \neq \emptyset\}$ .

## Gross Positive Prefix Lemma

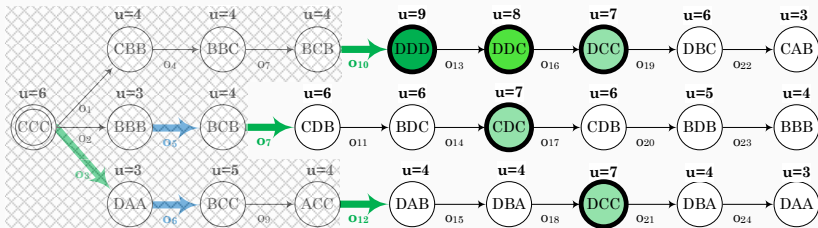
### Gross Positive Prefix



## Maintained Achievements Lemma

### Each improving plan over a given state

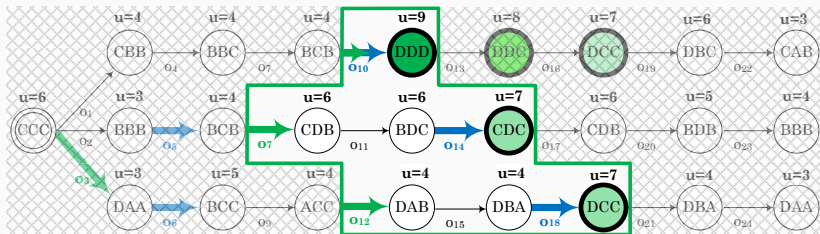
- starts with a gross positive action  $a_{gPos_1}$  and
- a valuable fact achieved by  $a_{gPos}$  is maintained along the suffix.



## The Window of Opportunity Theorem

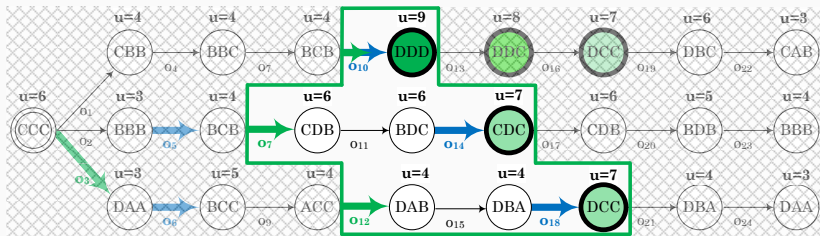
### synergistic criteria of optimal plan

- starts with a gross positive actions
- temporal maintained achievement
- terminates with a net positive action





## A Novel Landmarks Generation Approach



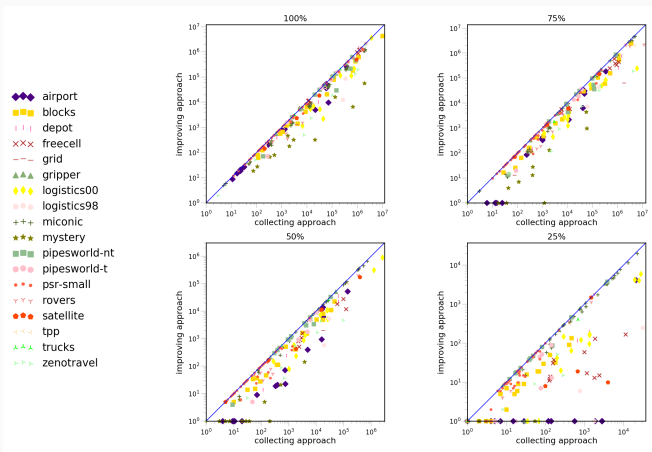
# Empirical Evaluation

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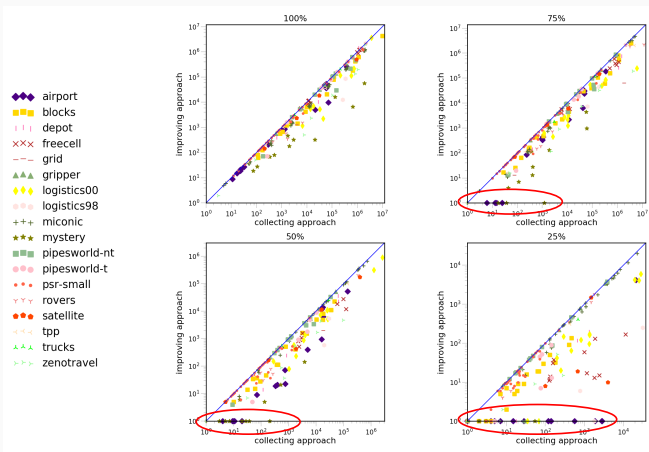
## Improving vs. Collecting Approach - Expanded Nodes

Utility setting  $u(\text{dom}(v)) \in \{0, 1, 2\}$



## Improving vs. Collecting Approach - Solved Without a Search

Utility setting  $u(\text{dom}(v)) \in \{0, 1, 2\}$



## Improving vs. Collecting Approach - Reduced Budget

Utility setting  $u(\text{dom}(v)) \in \{\{0, 1, 2\}\}$

	Reduced Budget		Discounted Actions		Effectiveness Score	
	<i>Improving</i>	<i>Collecting</i>	<i>Improving</i>	<i>Collecting</i>	<i>Improving</i>	<i>Collecting</i>
airport (17)	<b>484</b>	21	76318	<b>20375</b>	<b>157.68</b>	970.24
blocks (16)	<b>154</b>	18	215	<b>142</b>	<b>1.40</b>	7.89
depot (3)	<b>32</b>	3	569	<b>21</b>	17.78	<b>7.00</b>
freecell (11)	<b>54</b>	11	<b>5851</b>	15331	<b>108.35</b>	1393.73
grid (2)	<b>26</b>	15	2132	<b>1059</b>	82.00	<b>70.60</b>
gripper (4)	<b>60</b>	4	<b>172</b>	224	<b>2.87</b>	56.00
logistics00 (11)	<b>189</b>	11	212	<b>118</b>	<b>1.12</b>	10.73
logistics98 (3)	<b>40</b>	3	114	<b>40</b>	<b>2.85</b>	13.33
miconic (40)	<b>586</b>	121	2892	<b>1691</b>	<b>4.94</b>	13.98
mystery (11)	<b>49</b>	15	5142	<b>2122</b>	<b>104.94</b>	141.47
pipesw-nt (12)	<b>39</b>	28	<b>14751</b>	18500	<b>378.23</b>	660.71
pipesw-t (6)	<b>12</b>	6	9016	<b>5664</b>	<b>751.33</b>	944.00
psr-small (47)	<b>167</b>	55	2330	<b>1534</b>	<b>13.95</b>	27.89
rovers (6)	<b>44</b>	14	<b>380</b>	456	<b>8.64</b>	32.57
satellite (4)	<b>46</b>	10	264	<b>120</b>	<b>5.74</b>	12.00
tpp (6)	<b>62</b>	25	<b>155</b>	158	<b>2.50</b>	6.32
trucks (2)	<b>26</b>	7	<b>602</b>	931	<b>23.15</b>	133.00
zenotravel (8)	<b>57</b>	8	1213	<b>407</b>	<b>21.28</b>	50.88
total (209)	<b>2127</b>	375	122328	<b>68893</b>	<b>57.51</b>	183.71

## Negative Utility Setting

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Utility setting  $u(\text{dom}(v)) \in \{-1, 0, 1\}$

	25%			50%			75%			100%		
	Expanded	Solved	Time	Expanded	Solved	Time	Expanded	Solved	Time	Expanded	Solved	Time
airport (15)	0	15(15)	47.76	44599	15(6)	74.02	151860	15(6)	149.11	203372	15(0)	69.38
blocks (17)	405	17(4)	21.17	24379	17(1)	32.09	1945724	17(1)	144.81	14218611	17(1)	706.26
depot (3)	25	3(2)	11.42	16928	3(1)	17.38	382154	3(0)	43.46	13900	2(0)	8.88
freecell (5)	48	5(1)	77.51	2463	5(0)	122.81	14644	5(0)	132.95	24733	5(0)	141.51
grid (2)	0	2(2)	35.49	2021	2(1)	36.76	1142555	2(0)	111.88	1409996	2(0)	399.31
gripper (3)	821	3(1)	3.27	10258	3(0)	6.84	34214	3(0)	10.25	60207	3(0)	14.25
logistics00 10)	1043	10(2)	14.41	54470	10(0)	22.84	479866	10(0)	40.51	1854165	10(0)	108.12
logistics98 (2)	9	2(1)	1.97	10957	2(0)	3.98	94961	2(0)	8.23	327929	2(0)	21.95
miconic (40)	12746	40(15)	44.23	639797	40(6)	134.43	4748596	40(1)	425.22	11337706	40(0)	933.18
mystery (11)	0	11(11)	49.48	160	11(10)	51.71	12516	11(5)	67.39	395511	11(0)	121.13
pipesw-nt 11)	250	11(2)	48.19	21490	11(0)	99.09	290079	11(0)	178.4	2248028	11(0)	677.66
pipesw-t (5)	71	5(1)	45.68	6386	5(0)	71.05	95533	5(0)	88.71	356736	5(0)	115.91
rovers (4)	15	4(1)	2.6	7563	4(0)	5.58	2637	4(0)	5.18	10181	4(0)	7.21
satellite (4)	30	4(2)	4.53	13949	4(0)	9.97	187176	4(0)	24.52	1013108	4(0)	104.54
tpp (5)	0	5(5)	2.61	1932	5(1)	3.54	14455	5(1)	3.35	28278	5(0)	4.49
trucks (2)	730	2(1)	2.92	21946	2(0)	6	77382	2(0)	9.62	82969	2(0)	10.88
zenotravel (7)	34	7(4)	11.94	10594	7(1)	19.94	229144	7(1)	30.14	1477266	7(1)	85.49
total (146)	16227	146(70)	425.18	882892	146(27)	718.03	9903496	146(15)	1473.72	35062696	145(2)	3630.15



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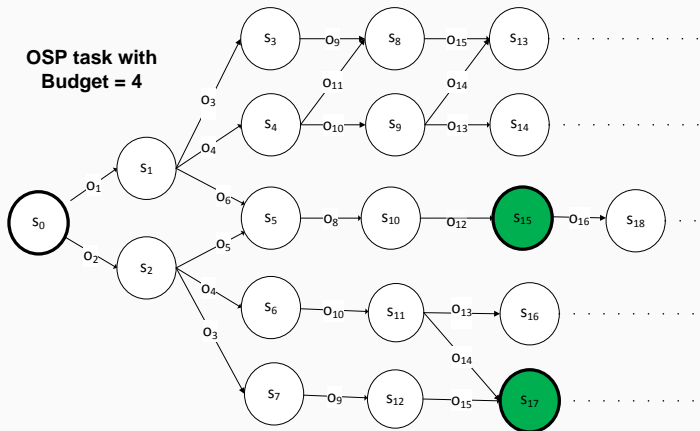


## Examples

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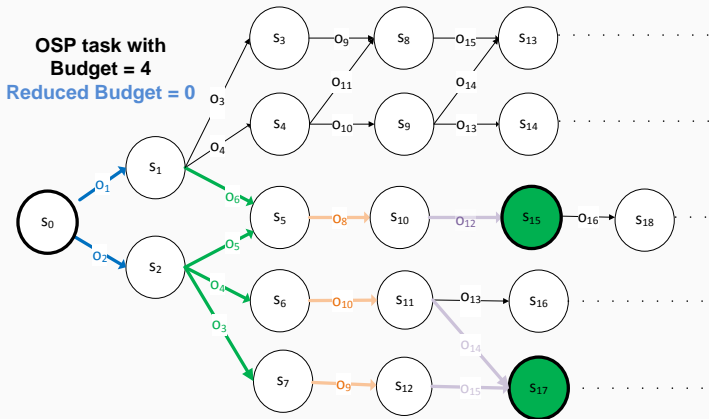
## Implications on Search Space

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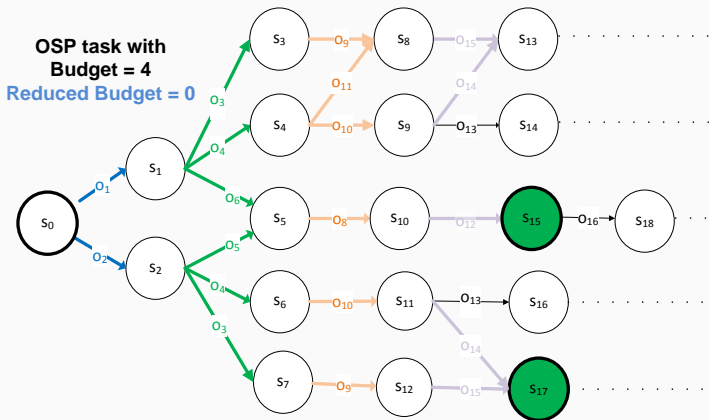
## Implications on Search Space

$$(a_1 \vee a_2) \wedge (a_3 \vee a_4 \vee a_5 \vee a_6) \wedge (a_8 \vee a_9 \vee a_{10}) \wedge (a_{12} \vee a_{14} \vee a_{15})$$



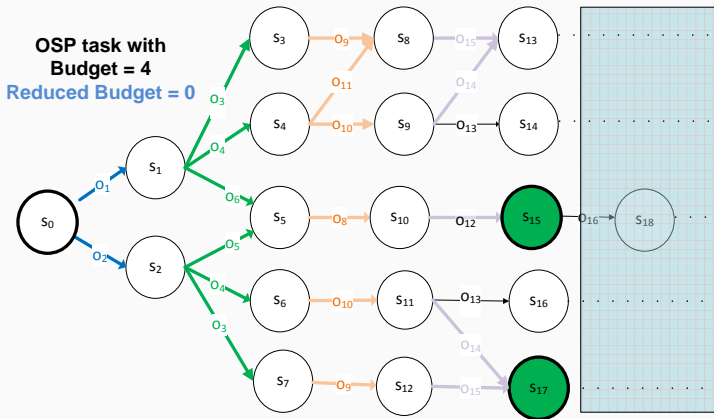
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$$(a_1 \vee a_2) \wedge (a_3 \vee a_4 \vee a_5 \vee a_6) \wedge (a_8 \vee a_9 \vee a_{10}) \wedge (a_{12} \vee a_{14} \vee a_{15})$$



## Implications on Search Space

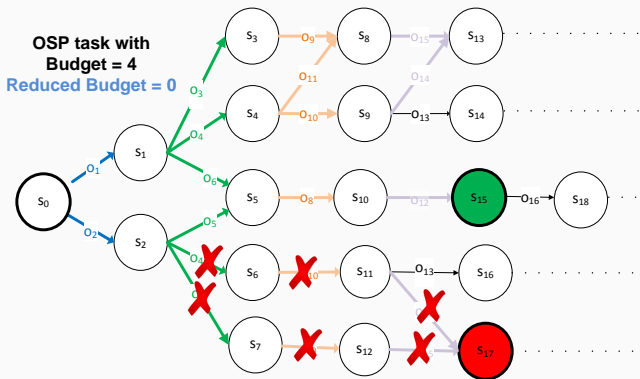
$$(a_1 \vee a_2) \wedge (a_3 \vee a_4 \vee a_5 \vee a_6) \wedge (a_8 \vee a_9 \vee a_{10}) \wedge (a_{12} \vee a_{14} \vee a_{15})$$



## Implications on Search Space

$$\overline{(a_1 \vee a_2) \wedge (a_3 \vee a_4 \vee a_5 \vee a_6) \wedge (a_8 \vee a_9 \vee a_{10}) \wedge (a_{12} \vee a_{14} \vee a_{15})}$$

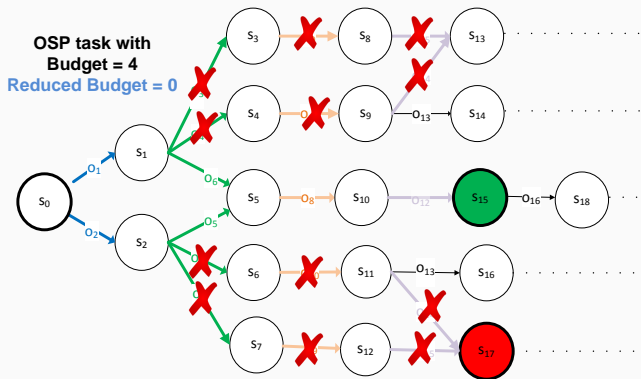
$$(a_1 \vee a_2) \wedge (a_5 \vee a_6) \wedge a_8 \wedge a_{13}$$



## Implications on Search Space

$$\overline{(a_1 \vee a_2) \wedge (a_3 \vee a_4 \vee a_5 \vee a_6) \wedge (a_8 \vee a_9 \vee a_{10} \vee a_{11}) \wedge (a_{14} \vee a_{15})}$$

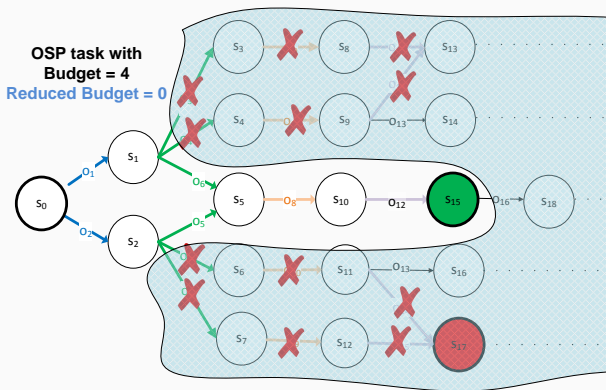
$$(a_1 \vee a_2) \wedge (a_5 \vee a_6) \wedge a_8 \wedge a_{13}$$



## Implications on Search Space

$$\overline{(a_1 \vee a_2) \wedge (a_3 \vee a_4 \vee a_5 \vee a_6) \wedge (a_8 \vee a_9 \vee a_{10} \vee a_{11}) \wedge (a_{14} \vee a_{15})}$$

$$(a_1 \vee a_2) \wedge (a_5 \vee a_6) \wedge a_8 \wedge a_{13}$$





## Example - Dynamic Relative Improvement Point

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$$\text{dom}(v_1) = \{at(pkg1, loc - A), at(pkg1, loc - B) \dots at(pkg1, loc - H)\}$$

$$\text{dom}(v_2) = \{at(pkg2, loc - A), at(pkg2, loc - B) \dots at(pkg2, loc - H)\}$$

•

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$$\text{dom}(v_7) = \{at(pkg7, loc - A), at(pkg7, loc - B) \dots at(pkg7, loc - H)\}$$

## Dynamic Relative Improvement Point

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A	170	12	8.5	0.6	-1.5	-10	-190
B	130	17	7.5	0.5	-5	-7	-140
C	140	11	8	0.2	-3.5	-5	-150
D	100	14	6.5	0.4	-3	-6	-200
E	150	10	7	0	-2.5	-4	-170
F	110	15	6	0.1	-4	-8	-180
G	120	16	5	0.7	-4.5	-9	-130
H	160	13	5.5	0.3	-2	-3	-160
	$v_1$	$v_2$	$v_3$	$v_4$	$v_5$	$v_6$	$v_7$

## Dynamic Relative Improvement Point

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170	12	8.5	0.6	-1.5	-10	-190
130	17	7.5	0.5	-5	-7	-140
140	11	8	0.2	-3.5	-5	-150
100	14	6.5	0.4	-3	-6	-200
150	10	7	0	-2.5	-4	-170
110	15	6	0.1	-4	-8	-180
120	16	5	0.7	-4.5	-9	-130
160	13	5.5	0.3	-2	-3	-160
$v_1$	$v_2$	$v_3$	$v_4$	$v_5$	$v_6$	$v_7$

## Dynamic Relative Improvement Point

---

170	17	8.5	0.7	-1.5	-3	-130
160	16	8	0.6	-2	-4	-140
150	15	7.5	0.5	-2.5	-5	-150
140	14	7	0.4	-3	-6	-160
130	13	6.5	0.3	-3.5	-7	-170
120	12	6	0.2	-4	-8	-180
110	11	5.5	0.1	-4.5	-9	-190
100	10	5	0	-5	-10	-200
$v_1$	$v_2$	$v_3$	$v_4$	$v_5$	$v_6$	$v_7$
$u(s^*)$				-39.8		

## Dynamic Relative Improvement Point

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170	17	8.5	0.7	-1.5	-3	-130
160	16	8	0.6	-2	-4	-140
150	15	7.5	0.5	-2.5	-5	-150
140	14	7	0.4	-3	-6	-160
130	13	6.5	0.3	-3.5	-7	-170
120	12	6	0.2	-4	-8	-180
110	11	5.5	0.1	-4.5	-9	-190
100	10	5	0	-5	-10	-200

$v_1$	$v_2$	$v_3$	$v_4$	$v_5$	$v_6$	$v_7$
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$u(s^*)$	-35.3
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## Dynamic Relative Improvement Point

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170	17	8.5	0.7	-1.5	-3	-130
160	16	8	0.6	-2	-4	-140
150	15	7.5	0.5	-2.5	-5	-150
140	14	7	0.4	-3	-6	-160
130	13	6.5	0.3	-3.5	-7	-170
120	12	6	0.2	-4	-8	-180
110	11	5.5	0.1	-4.5	-9	-190
100	10	5	0	-5	-10	-200

$v_1$	$v_2$	$v_3$	$v_4$	$v_5$	$v_6$	$v_7$
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$u(s^*)$	-20.3
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## Dynamic Relative Improvement Point

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170	17	8.5	0.7	-1.5	-3	-130
160	16	8	0.6	-2	-4	-140
150	15	7.5	0.5	-2.5	-5	-150
140	14	7	0.4	-3	-6	-160
130	13	6.5	0.3	-3.5	-7	-170
120	12	6	0.2	-4	-8	-180
110	11	5.5	0.1	-4.5	-9	-190
100	10	5	0	-5	-10	-200

$v_1$	$v_2$	$v_3$	$v_4$	$v_5$	$v_6$	$v_7$
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$u(s^*)$	12
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## Dynamic Relative Improvement Point

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170	17	8.5	0.7	-1.5	-3	-130
160	16	8	0.6	-2	-4	-140
150	15	7.5	0.5	-2.5	-5	-150
140	14	7	0.4	-3	-6	-160
130	13	6.5	0.3	-3.5	-7	-170
120	12	6	0.2	-4	-8	-180
110	11	5.5	0.1	-4.5	-9	-190
100	10	5	0	-5	-10	-200

$v_1$	$v_2$	$v_3$	$v_4$	$v_5$	$v_6$	$v_7$
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$u(s^*)$	18.5
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## Dynamic Relative Improvement Point

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170	17	8.5	0.7	-1.5	-3	-130
160	16	8	0.6	-2	-4	-140
150	15	7.5	0.5	-2.5	-5	-150
140	14	7	0.4	-3	-6	-160
130	13	6.5	0.3	-3.5	-7	-170
120	12	6	0.2	-4	-8	-180
110	11	5.5	0.1	-4.5	-9	-190
100	10	5	0	-5	-10	-200

$v_1$	$v_2$	$v_3$	$v_4$	$v_5$	$v_6$	$v_7$
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$u(s^*)$	51.7
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THANK YOU

